



**EEL 5245 POWER ELECTRONICS I**  
**Lecture #11: Chapter 4**  
**DC-DC and Review of Ch 2-3**



# Objectives

- Review of Ch2-3 topics
- Overview of DC-DC Conversion
  - Linear Regulators: Regulated vs. Unregulated
  - Overview of Pulse Width Modulation Converters
- PWM Converter Analysis Principles/Tools
  - Duty Ratio
  - Steady-State
  - Inductor Volt-Second Balance
  - Capacitor charge balance
  - Small Ripple Approximation
  - Conservation of Power



## Key Topics from Chapter 2

- Significance of Switching in Power Electronics
- Ideal Switch Characteristics
- Practical Switch Limitations
- Power Loss in Practical Switch
  - Switching Losses
  - Conduction Loss
- Calculation of Switch Loss from V&I Waveforms
- Calculation  $P_{\max}$  (instantaneous maximum power) from V&I Waveforms
- Semiconductor Devices
  - Device types, function, and current/voltage carry/block.



## Key Topics from Chapter 2- Cont

- **Figures of Merit (Definitions/Lingo)**
  - On state resistance, forward voltage drop, reverse blocking capability, switching time, etc.
- **Qualitative Relationships**
  - Family to family comparisons (which device is best for a particular application)
    - e.g. MOSFETs faster than BJT
  - Figures of merit comparison within family
    - e.g. Higher reverse blocking, higher on-state resistance



## Key Topics from Chapter 3

- Solution of First and Second Order Diff Eq.s by Laplace and Method of Undetermined Coefficients
- Be able to solve any class example and focus on:
  - Mode by mode analysis
  - Energy Transfer from Input to Output
  - Energy exchange from/to reactive elements
  - Initial and final conditions of state variables
  - Continuity of state variables
  - Energy conservation
  - Current commutation
  - Current Freewheeling



# Key Topics from Chapter 3

- Output Voltage Ripple
- Inductor Current Ripple
- Load and Line Regulation
- Small Ripple Approximation
- Steady-state definition
- Inductor Volt-Sec Balance
- Capacitor Charge Balance
- Use of Diodes/Switches to control flow of energy and regulate output voltage
- Integration Tips and Tricks (Time shift to simplify)



# Key Topics from Chapter 3- Cont

- **Sinusoidal Systems and Basic Power Concepts**
  - Understand and be able to apply basic power concepts to solution of problems involving sinusoidal systems and to some extent non-sinusoidal systems
    - Basic Definitions of average, instantaneous power
    - RMS definition
    - Application of basic integral formulas to commonly observed Power Electronics Waveforms
    - Power Factor Concepts and Correction

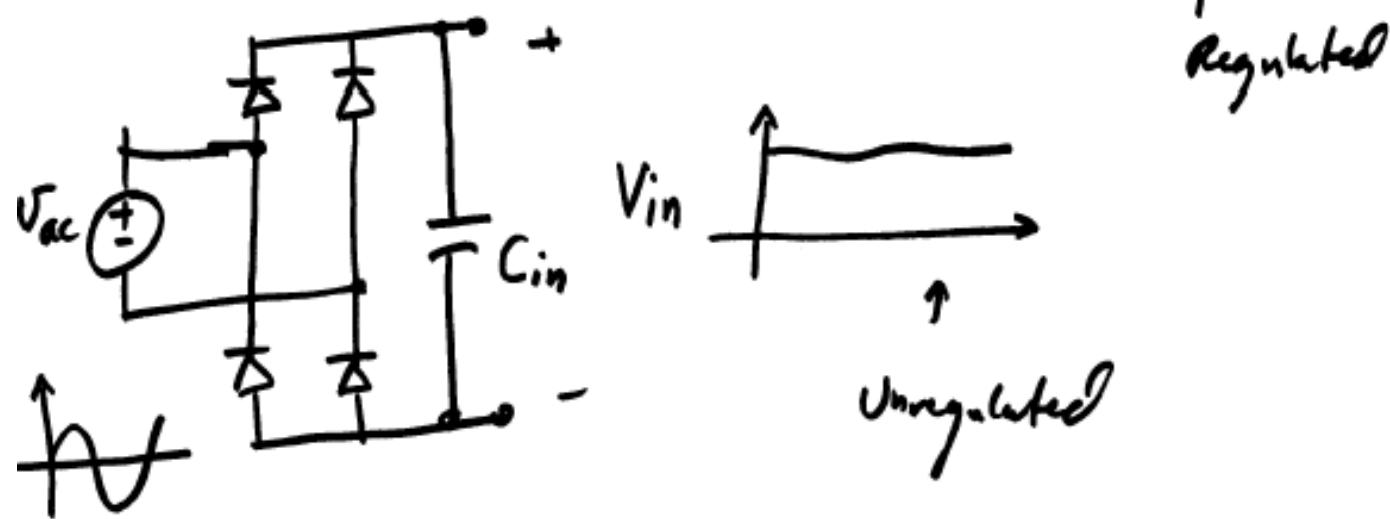


# Key Topics from Chapter 3- Cont

- **Non-Sinusoidal Systems, Harmonics and Fourier Analysis**
  - Understand and be able to apply Fourier Analysis to obtain harmonic content of any periodic waveform
    - Both forms of Fourier Series from class
  - Real, Apparent, and Reactive Power in the Nonsinusoidal system
  - Power Factor, distortion factor, displacement factor
  - THD
  - RMS calculation with nonsinusoidal waveforms
  - Understand the effects of Harmonics
    - Neutral currents,  $I^2R$  heating, measurement error, etc.



# Overview of DC to DC Conversion





# Overview of Linear Regulator

Block diagram for a linear-regulator

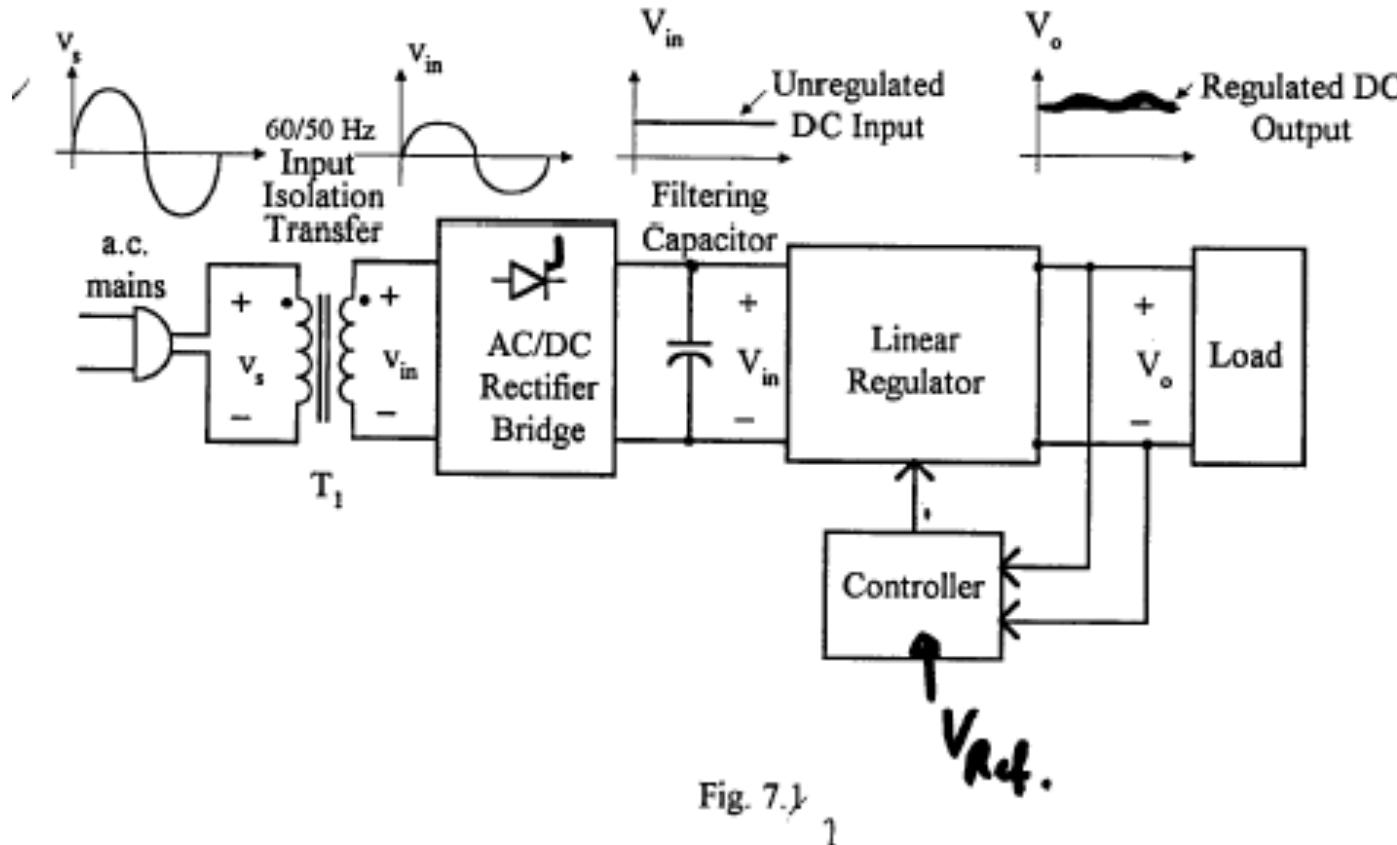
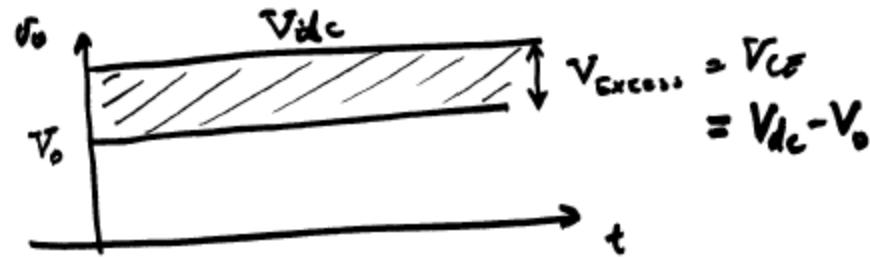
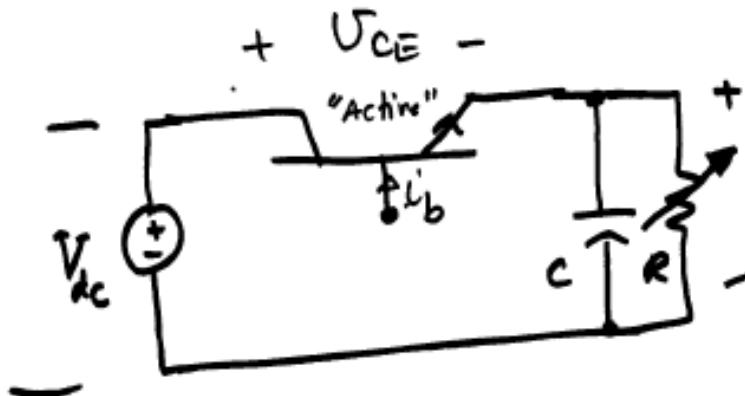


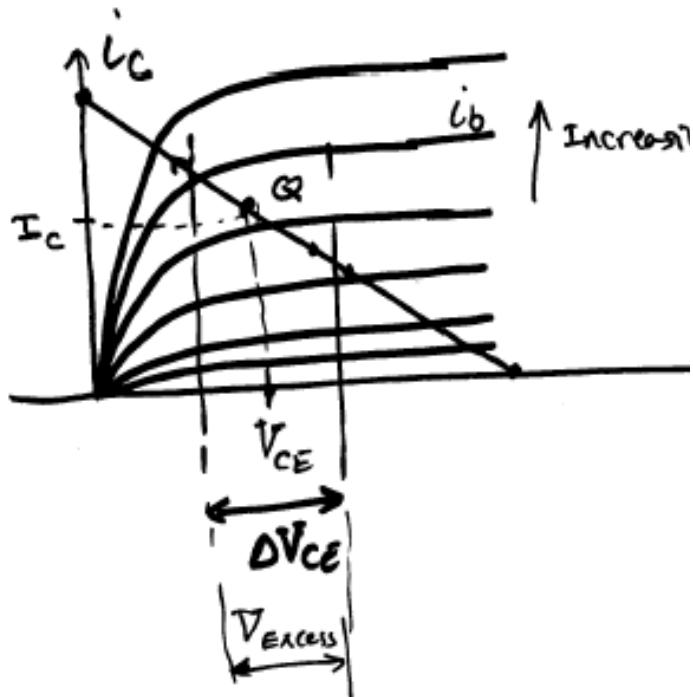
Fig. 7.1  
1



# Efficiency of Linear Regulator



$V_{CE} = V_{excess} \Leftrightarrow$  The wasted voltage across the linear element (transistor).



$$V_0 = V_{dc} - V_{excess}$$

↑

Controlled by Varying  $i_b$ .



# Comments on Linear Regulator

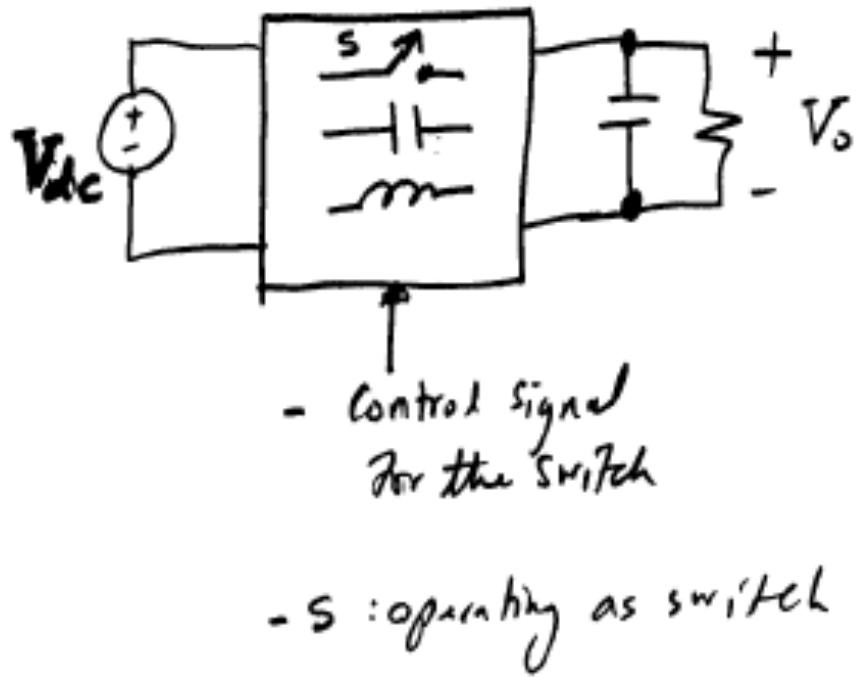
## Features:

- Simple Topology (No switching) + low GMII
- Easy to understand (active mode) (single loop) + reliable!
- Linear operation for the active device.
- Very high power dissipation (low efficiency)  
 $\eta = 50\%$
- low power applications.



# PWM Converter Overview

PWM Switch-Mode Converters  
Pulse Width Modulation (PWM)



**mod·u·late**

v/i)

v. **mod·u·lat·ed, mod·u·lat·ing, mod·u·lates**

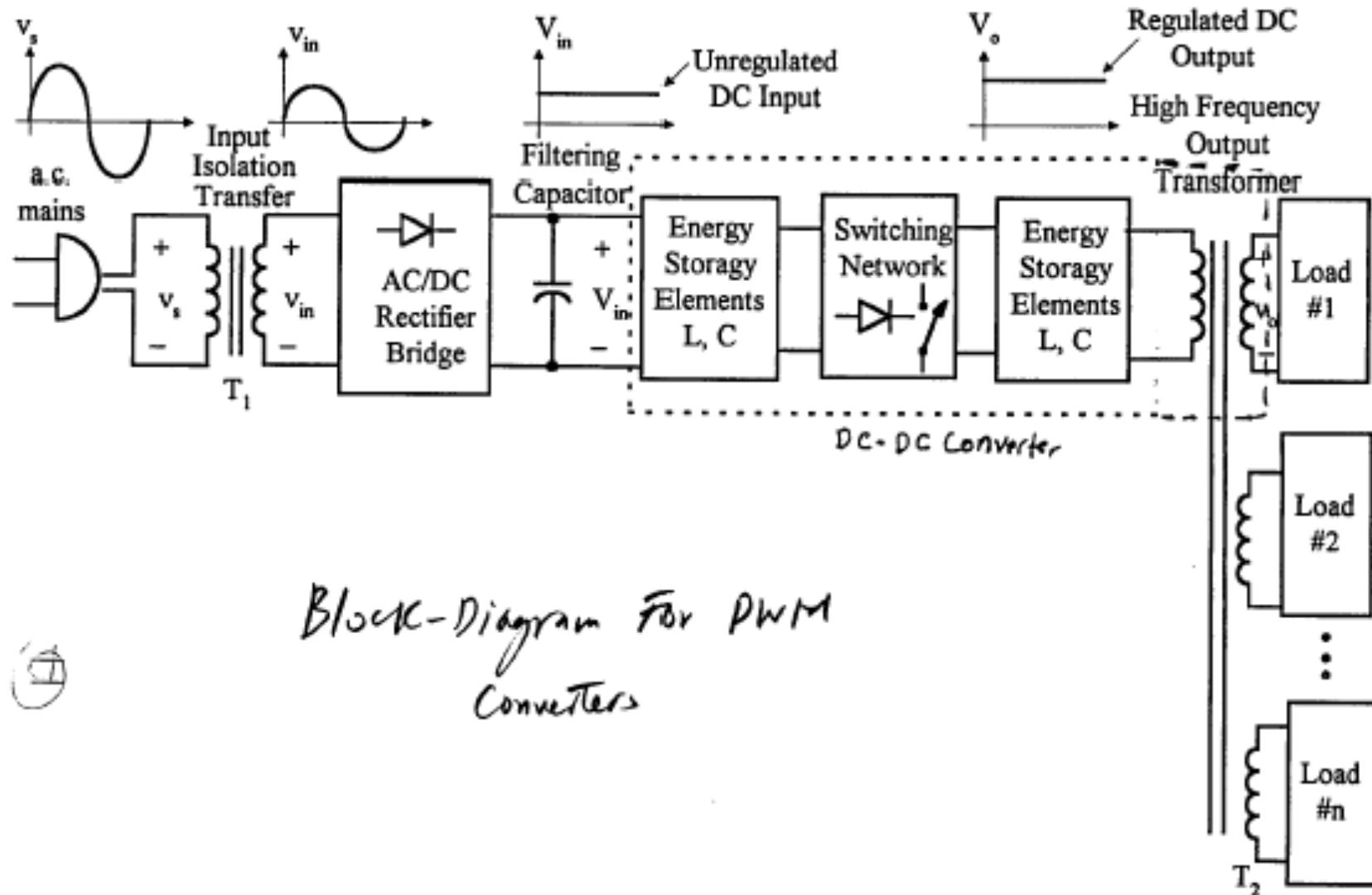
v. *tr.*

1. Electronics.

a. To vary the frequency, amplitude, phase, or other characteristic of (electromagnetic waves).



# PWM Converter Overview





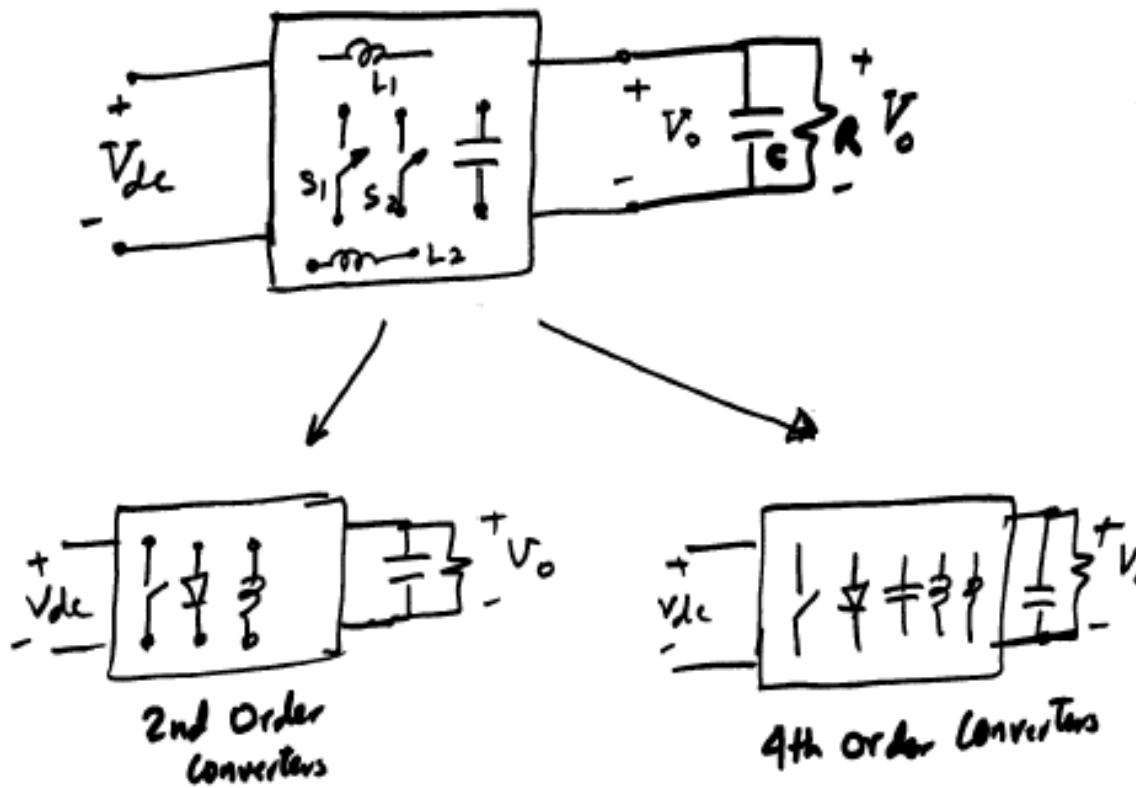
# PWM Converter Overview

## Features of PWM Converters:

- Simple Topologies (one switch)
- Well understood operation / control.
- Simple Control Circuit.
- Wide power applications
- High Efficiency converter (90%).
- ~~Variable~~ <sup>Fixed</sup> switching frequency (filtering easy)  
[Low Harmonics]



# PWM Converter Overview



Example:

- Buck Converter (Step down)
- Boost Converter (Step up)
- Buck-Boost converter  
(Step up/down)

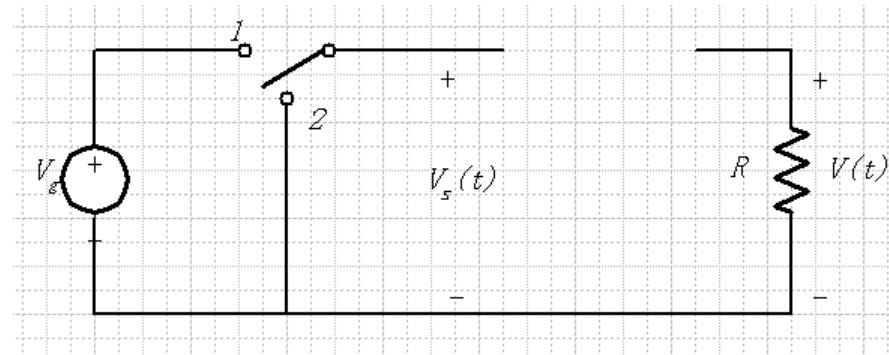
Example:

- Cuk
- Zeta
- SEPIC



# PWM Switching

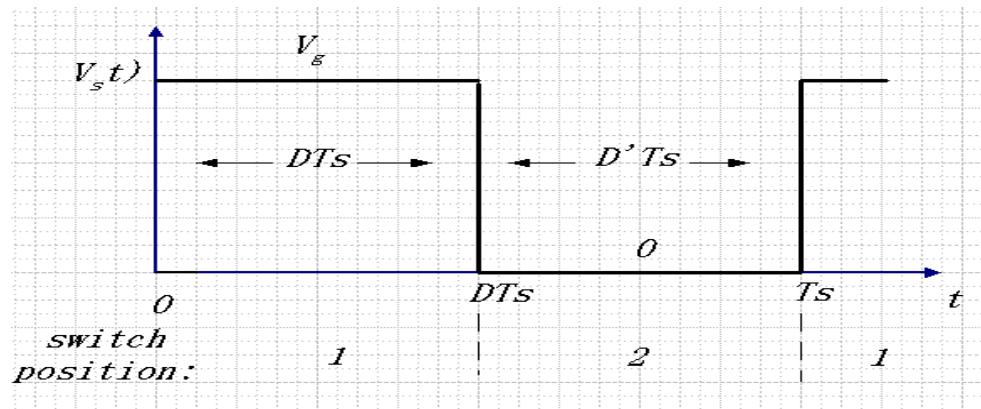
*SPDT switch changes dc component*



*Switch output voltage waveform*

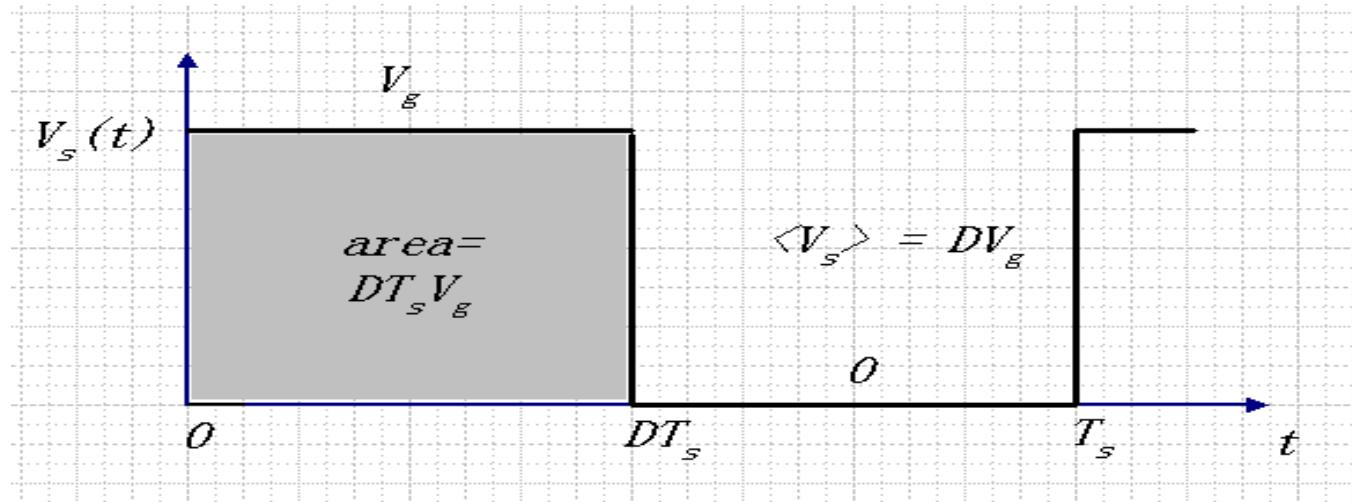
Duty cycle  $D$ :  
 $0 \leq D \leq 1$

complement  $D'$ :  
 $D' = 1 - D$





# Output Voltage Average Value (Buck)



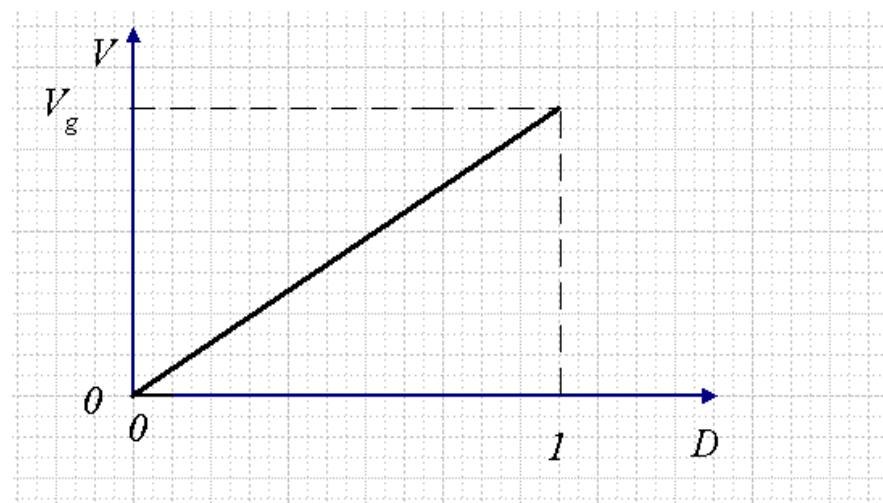
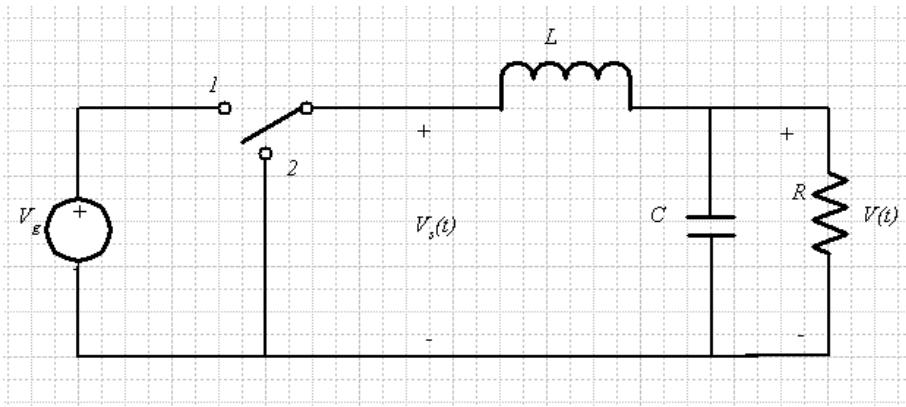
*Fourier analysis: Dc component = average value*

$$\langle v_s \rangle = \frac{1}{T_s} \int_0^{T_s} v_s(t) dt$$

$$\langle v_s \rangle = \frac{1}{T_s} (DT_s V_g) = DV_g$$



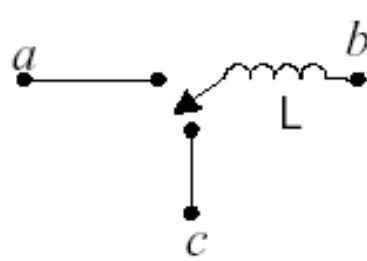
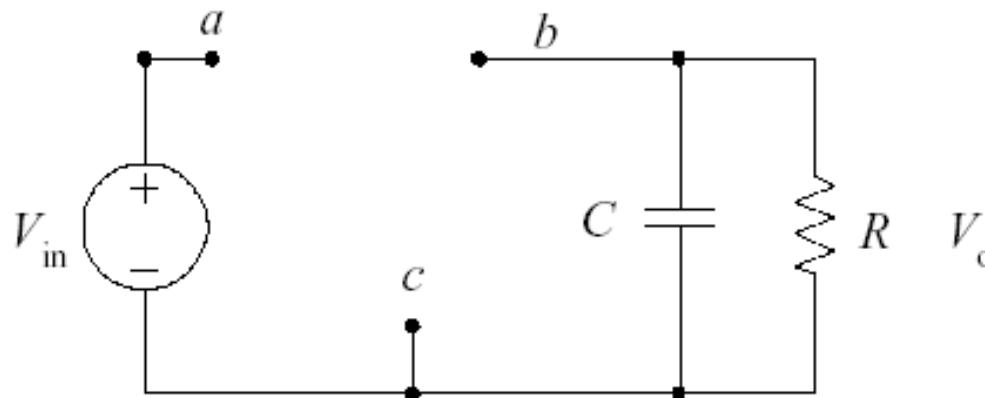
# Buck Converter



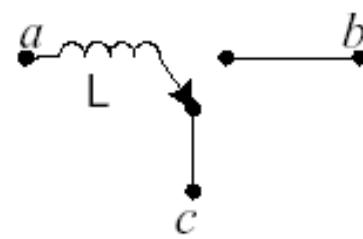
- **Switch Position 2** for allow for uninterrupted inductor current flow
- **LPF for smoothing of pulse for constant DC output**
- **Capacitor hold a DC value for the load when switch in position 1 (Inductor current charge)**
- **2<sup>nd</sup> Order-1 L, 1 C**



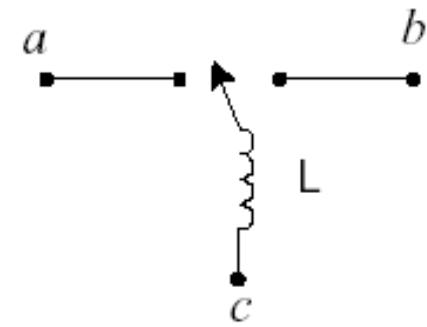
# Derivation of Classic Converter Topologies (2<sup>nd</sup> Order)



(a)



(b)

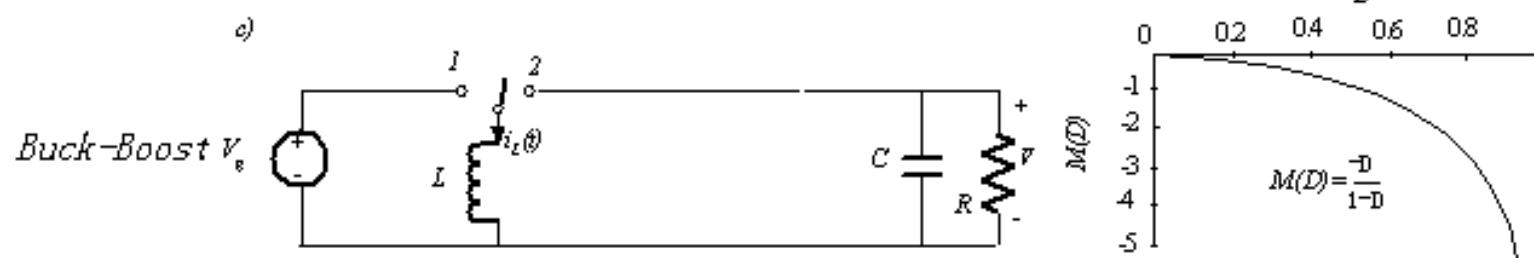
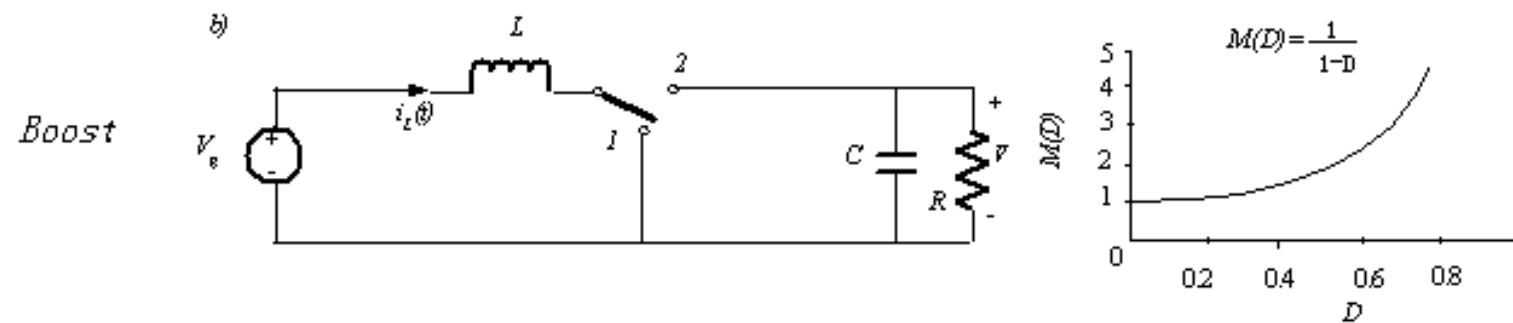
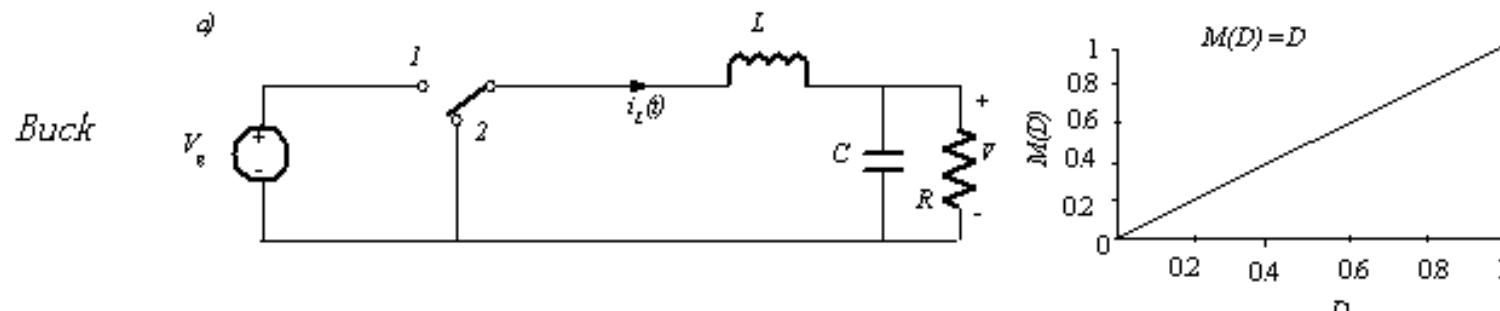


(c)

Figure 4.8: Low-pass LC filter (a) buck (b) boost (c) buck boost converter



# Classic Converter Topologies





# Analysis of Classic Converter Topologies

- Analysis will assume lossless components
- Exact steady state analysis would involve solution of nonlinear, 2nd Order system, we will simplify to a 1<sup>st</sup> Order System with:
  - Since  $RC \gg Ts$ , output voltage nearly constant over switching period
    - Since ripple is assumed small, we assume  $V_o$  a constant during analysis (output cap not considered)
- We assume analysis of converter takes place at after it has reached steady state
  - Since steady state, average inductor voltage equals zero over switching interval (volt-sec balance)
  - Since steady state, average capacitor current over one switching interval equals zero (charge balance)



# Analysis of Classic Converter Topologies

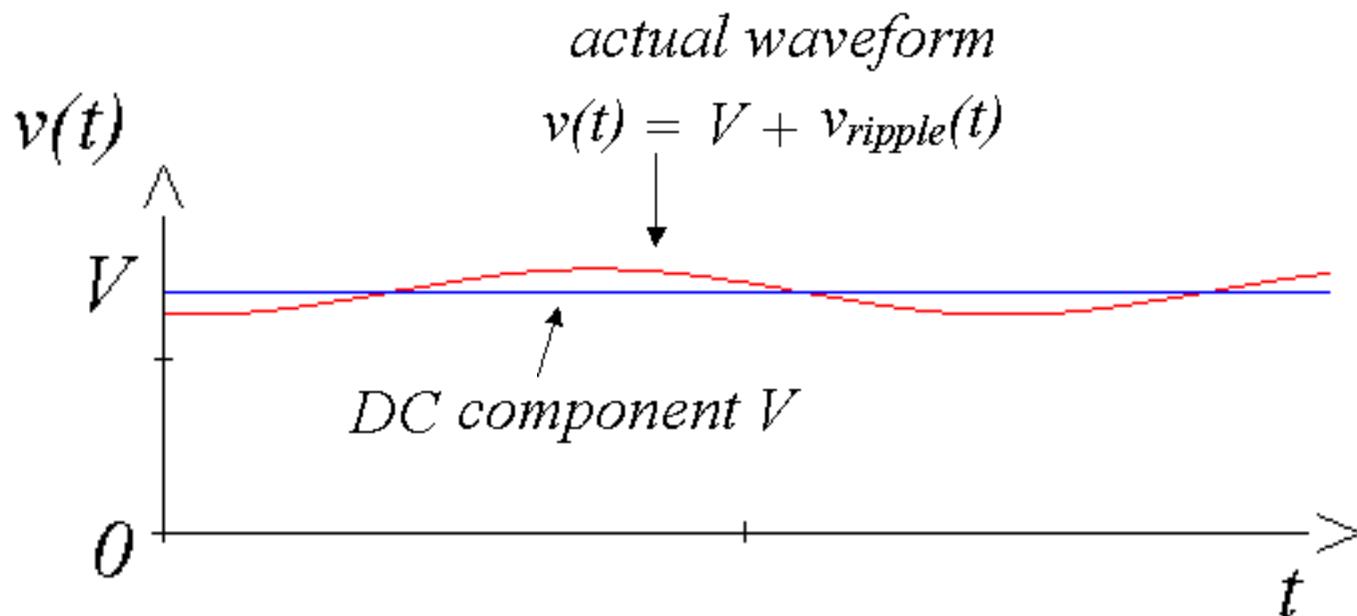
- The preceding concepts can be expressed in terms of mathematical relations.
- These are tools for analysis:
  - $P_{\text{out}} = P_{\text{in}}$  (Power Conservation)
  - $i_L(t_0) = i_L(t_0 + T_s)$  (Steady State)
  - $I_{\text{cavg}} = 0$  (Charge Balance)
  - $V_{L\text{avg}} = 0$  (volt-sec balance)

$$I_c = \frac{1}{T} \int_{t_0}^{T+t_0} i_c(t) dt = 0$$

$$V_L = \frac{1}{T} \int_{t_0}^{T+t_0} v_L(t) dt = 0$$



# Converter Analysis Principle Small Ripple Approximation



In a well-designed converter, the output voltage ripple is small. Hence, the waveforms can be easily determined by ignoring the ripple:

$$|v_{\text{ripple}}| \ll V$$

$$v(t) \approx V$$



# Converter Analysis Principle

## Inductor Volt-Second Balance

**Inductor defining relation :**

$$v_L(t) = L \frac{di_L(t)}{dt}$$

**Integrate over one complete switching period :**

$$i_L(T_s) - i_L(0) = \frac{1}{L} \int_0^{T_s} v_L(t) dt$$

**In periodic steady state, the net change in inductor current is zero :**

$$0 = \int_0^{T_s} v_L(t) dt$$

**Hence, the total area (or volt-seconds) under the inductor voltage waveform is zero whenever the converter operates in steady state.**

**An equivalent form:**

$$0 = \frac{1}{T} \int_0^{T_s} v_L(t) dt = \langle v_L \rangle$$

**The average inductor voltage is zero in steady state**

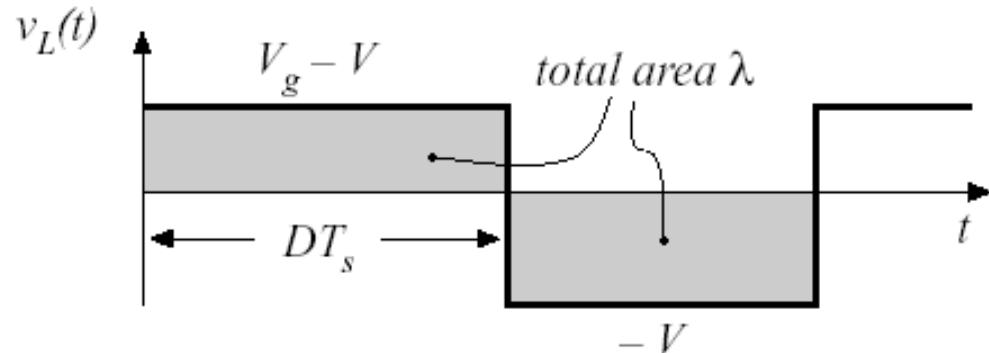


# Converter Analysis Principle

## Volt-Second Balance

### gives Voltage Gain, M

Inductor voltage waveform,  
previously derived:



Integral of voltage waveform is area of rectangles:

$$\lambda = \int_0^{T_s} v_L(t) dt = (V_g - V)(DT_s) + (-V)(D'T_s)$$

Average voltage is

$$\langle v_L \rangle = \frac{\lambda}{T_s} = D(V_g - V) + D'(-V)$$

Equate to zero and solve for  $V$ :

$$0 = DV_g - (D + D')V = DV_g - V \quad \Rightarrow \quad V = DV_g$$

Example is for Buck



# Converter Analysis Principle Capacitor Charge Balance

**Capacitor defining relation:**

$$i_c(t) = C \frac{dv_c(t)}{dt}$$

**Integrate over one complete switching period**

$$v_c(T_s) - v_c(0) = \frac{1}{C} \int_0^{T_s} i_c(t) dt$$

**in periodic steady state, the net change in capacitor voltage is zero:**

$$0 = \frac{1}{T} \int_0^{T_s} i_c(t) dt = \langle i_c \rangle$$

**Hence, the area (or charge) under the capacitor current waveform is zero whenever the converter operates in steady state. The average capacitor current is then zero.**



# Figures of Merit for the PWM DC-DC Converter

## “Plan of Attack”

- Classic Converter Analysis (CCM)
  - Voltage Conversion Ratio ( $M=Gain$ )
    - Use Inductor Volt-second balance
  - Average Input and Output Currents
    - Use waveform analysis and
    - Capacitor charge balance and small ripple approximation ( $I_{cavg}=0$ )
  - Output Voltage Ripple via Charge approximation
    - Small ripple approximation means all ac component of output current seen by capacitor, DC to load  $R$
  - Inductor current Ripple
    - Derived from inductor current waveform
  - Boundary Between CCM and DCM
    - Concept of Critical Inductance derived from  $i_L$  expressions